

التمرين الأول

(1)

$D = \sqrt{2+\sqrt{3}} \times \sqrt{2-\sqrt{3}}$ $= \sqrt{(2+\sqrt{3})(2-\sqrt{3})}$ $= \sqrt{(2)^2 - (\sqrt{3})^2}$ $= \sqrt{4-3}$ $= \sqrt{1}$ $= 1$	$B = \sqrt{28} - \frac{1}{3}\sqrt{63} + \sqrt{175}$ $= \sqrt{2^2 \times 7} - \frac{1}{3}\sqrt{3^2 \times 7} + \sqrt{5^2 \times 7}$ $= 2\sqrt{7} - \sqrt{7} + 5\sqrt{7}$ $= (2-1+5)\sqrt{7}$ $= 6\sqrt{7}$	$A = \sqrt{15} \times \sqrt{12} \times \sqrt{5}$ $= \sqrt{5 \times 3} \times \sqrt{2^2 \times 3} \times \sqrt{5}$ $= \sqrt{5} \times \sqrt{3} \times 2\sqrt{3} \times \sqrt{5}$ $= (\sqrt{5})^2 \times (\sqrt{3})^2 \times 2$ $= 5 \times 3 \times 2$ $= 30$
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$$C = \frac{(x^2 y^{-4})^{-2} z}{x^2 (y^{-4} z)^{-1}}$$

$$= \frac{x^{-4} y^8 z}{x^2 y^4 z^{-1}}$$

$$= \frac{y^{8-4} z^{1-(-1)}}{x^{2-(-4)}}$$

$$= \frac{y^4 z^2}{x^6}$$

$$= x^{-6} y^4 z^2$$

(2)

$$\sqrt{43+30\sqrt{2}} = \sqrt{(3\sqrt{2}+5)^2} \quad (3\sqrt{2}+5)^2 = (3\sqrt{2})^2 + 2 \times (3\sqrt{2}) \times 5 + (5)^2$$

$$= |3\sqrt{2}+5| \quad \text{إذن} \quad = 18 + 30\sqrt{2} + 25$$

$$= 3\sqrt{2}+5 \quad = 43 + 30\sqrt{2}$$

(3)

$$F = 1445,45$$

$$= 1,44545 \times 10^{-3}$$

$$F = \frac{(0,0005)^2 \times (0,002)^4 \times 60}{(10^{-2})^{-2}}$$

$$= \frac{5 \times 10^{-4} \times 2 \times 10^{-3} \times 6 \times 10}{10^4}$$

$$= 6 \times (5 \times 2) \times 10^{-4-3+1-4}$$

$$= 6 \times 10 \times 10^{-10}$$

$$= 6 \times 10^{1-10}$$

$$= 6 \times 10^{-9}$$

$$AB^2 + BC^2 = (\sqrt{5})^2 + (\sqrt{11})^2 \quad (4)$$

$$= 5 + 11 \quad \text{بما أن}$$

$$= 16$$

$$= AC^2$$

فإن ABC قائم الزاوية في الرأس B

التمرين الثاني

$$(1)$$

$$4\sqrt{7} > 7\sqrt{2} \quad \text{بما أن } (7\sqrt{2})^2 = 49 \times 2 = 98 \quad \text{و} \quad (4\sqrt{7})^2 = 16 \times 7 = 112 \cdot$$

$$\left(\sqrt{4\sqrt{7}-2}\right)^2 - \left(\sqrt{7\sqrt{2}-3}\right)^2 = (4\sqrt{7}-2) - (7\sqrt{2}-3)$$

$$= (4\sqrt{7}-7\sqrt{2})+1 \quad \cdot \text{ لدينا :}$$

$$\text{نعلم أن } 4\sqrt{7} > 7\sqrt{2} \quad \text{أي } 4\sqrt{7}-7\sqrt{2} > 0 \quad \text{إذن } \left(\sqrt{4\sqrt{7}-2}\right)^2 - \left(\sqrt{7\sqrt{2}-3}\right)^2 > 0 \quad \text{ومنه فإن}$$

$$\sqrt{4\sqrt{7}-2} > \sqrt{7\sqrt{2}-3} \quad \text{وكذلك } \left(\sqrt{4\sqrt{7}-2}\right)^2 > \left(\sqrt{7\sqrt{2}-3}\right)^2$$

$$(2)$$

$$\cdot -3 \leq x + y \leq 1$$

$$\cdot -7 \leq x - y \leq -3 \quad \text{إذن } -3 \leq -y \leq -1 \quad \text{و} \quad -4 \leq x \leq -2 \cdot$$

$$\cdot -12 \leq xy \leq -2 \quad \text{أي } 2 \leq -xy \leq 12 \quad \text{إذن } 1 \leq y \leq 3 \quad \text{و} \quad 2 \leq -x \leq 4 \cdot$$

$$\bullet \quad -4 \leq \frac{x}{y} \leq \frac{-2}{3} \text{ أي } \frac{2}{3} \leq \frac{-x}{y} \leq 4 \text{ إذن } \frac{1}{3} \leq \frac{1}{y} \leq 1 \text{ و } 2 \leq -x \leq 4$$

$$\bullet \quad \frac{1}{17} \leq \frac{1}{x^2+1} \leq \frac{1}{5} \text{ أي } 5 \leq x^2+1 \leq 17 \text{ إذن } 4 \leq x^2 \leq 16 \text{ وكذلك } 1 \leq x+5y \leq 13 \text{ إذن } 5 \leq 5y \leq 15$$

$$\text{عليه فإن } \frac{1}{17} \leq \frac{x+5y}{x^2+1} \leq \frac{13}{5}$$

التمرين الثالث

$$5x+2x=3+4 \text{ تكافئ } 5x-4=-2x+3$$

$$7x=7 \text{ تكافئ}$$

$$x=1 \text{ تكافئ}$$

اتمم.....

$$3x+2x \leq -2-6 \text{ تكافئ } 3(x+2) \leq -2(x+1)$$

$$5x \leq -8 \text{ تكافئ}$$

$$x \leq \frac{-8}{5} \text{ تكافئ}$$

اتمم.....

$$(3x+5)^2 - (x-2)^2 = 0 \text{ تكافئ } (3x+5)^2 = (x-2)^2$$

$$[(3x+5)+(x-2)][(3x+5)-(x-2)] = 0 \text{ تكافئ}$$

$$(4x+3)(2x+7) = 0 \text{ تكافئ}$$

$$(2x+7) = 0 \text{ أو } (4x+3) = 0 \text{ تكافئ}$$

$$\text{تكمافئ } x = -\frac{7}{2} \text{ أو } x = -\frac{3}{4} \text{ أتمم.....}$$